



Extension of ACM for Computing the Geometric Progression

Chinnaraji Annamalai^{1*}

¹School of Management, Indian Institute of Technology, Kharagpur, India.

Article Information

DOI: 10.9734/JAMCS/2019/v31i530125

Editor(s):

(1) Chin-Chen Chang, Professor, Department of Information Engineering and Computer Science, Feng Chia University, Taiwan.

Reviewers:

(1) Alcínia Zita Sampaio, Technical University of Lisbon, Portugal.

(2) Ayman shehata Mohammed Ahmed El-Shazly, Assiut University, Egypt.

(3) Irina Dorca, University of Pitesti, Romania.

Complete Peer review History: <http://www.sdiarticle3.com/review-history/10860>

Received: 12 February 2014

Accepted: 19 June 2014

Published: 06 April 2019

Short Research Article

Abstract

This paper presents a novel approach to ACM-geometric progression [1,3] and it is very useful for research in science and technology [3].

Keywords: ACM-geometric progression; Annamalai theorem.

1 Introduction

Annamalai theorems [1,2] or Annamalai computing models (ACM) [3] play key roles in research fields such as computer science, information systems, electrical & electronics, medicine, computational biology, etc.

Annamalai Theorems

$$\sum_{i=k}^{n-1} 2^i = 2^n - 2^k \quad (1)$$

$$\sum_{i=k}^{n-1} 3^i = \frac{3^n - 3^k}{2} \quad (2)$$

*Corresponding author: anna@iitkgp.ac.in;

$$\sum_{i=k}^{n-1} 4^i = \frac{4^n - 4^k}{3} \tag{3}$$

.....

$$m-1) \sum_{i=k}^{n-1} m^i = \frac{m^n - m^k}{m - 1}$$

Proof :

Theorem 1:

$$\sum_{i=k}^{n-1} 2^i = 2^n - 2^k$$

[1, 3]

Please refer to my journal paper entitled “A novel computational technique for the geometric progression of powers of two” in the reference section.

The other theorems can be proved as above [1].

Theorem 2:

$$\begin{aligned} 3^n &= 3^n \\ 3^n &= 3^{n-1} + 3^{n-1} + 3^{n-1} \\ 3^n &= 2(3^{n-1}) + 3^{n-2} + 3^{n-2} + 3^{n-2} \end{aligned}$$

Similarly, we can continue this mathematical expression as follows

$$\begin{aligned} 3^n &= 2(3^{n-1}) + 2(3^{n-2}) + 2(3^{n-3}) + \dots + 2(3^i) + \dots + 2(3^k) + 3^k \\ \therefore \sum_{i=k}^{n-1} 3^i &= \frac{3^n - 3^k}{2} \end{aligned}$$

Theorem 3:

$$\begin{aligned} 4^n &= 4^n \\ 4^n &= 4^{n-1} + 4^{n-1} + 4^{n-1} + 4^{n-1} \\ 4^n &= 3(4^{n-1}) + 4^{n-2} + 4^{n-2} + 4^{n-2} + 4^{n-2} \end{aligned}$$

Similarly, we can continue this mathematical expression as follows

$$\begin{aligned} 4^n &= 3(4^{n-1}) + 3(4^{n-2}) + 3(4^{n-3}) + \dots + 3(4^i) + \dots + 3(4^k) + 4^k \\ \therefore \sum_{i=k}^{n-1} 4^i &= \frac{4^n - 4^k}{3} \end{aligned}$$

.....

Theorem (m-1) [2]:

$$m^n = m^n$$

$$m^n = m^{n-1} + m^{n-1} + \dots + m^{n-1} \quad (\text{m times})$$

$$m^n = (m-1)(m^{n-1}) + (m-1)(m^{n-2}) + (m-1)(m^{n-3}) + \dots + (m-1)m^i + \dots + (m-1)m^k + m^k$$

$$\therefore \sum_{i=k}^{n-1} m^i = \frac{m^n - m^k}{m - 1}$$

2 Conclusion

In the research study, ACM [1,2,3] will be very useful for researchers involving in broad research areas such as computer science, information systems, electrical & electronics, biomedicine, computational biology, etc.

Competing Interests

Author has declared that no competing interests exist.

References

- [1] Annamalai C. A novel computational technique for the geometric progression of powers of two. Journal of Scientific and Mathematical Research. 2009;3:16-17.
- [2] Annamalai C. A novel method for generic geometric progression. International Journal of Computational and Applied Mathematics. 2010;5(6):779-781.
- [3] Annamalai C. ACM cryptographic key exchange for secure communications. International Journal of Cryptology Research. 2011;3(1):27-33.

© 2019 Annamalai; This is an Open Access article distributed under the terms of the Creative Commons Attribution License (<http://creativecommons.org/licenses/by/3.0>), which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.

Peer-review history:
 The peer review history for this paper can be accessed here (Please copy paste the total link in your browser address bar)
<http://www.sdiarticle3.com/review-history/10860>